

## ***An Empirical Investigation of Cost Efficiency in the Banking Sector of Pakistan***

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*This study uses the distribution free approach to estimate levels of cost efficiency of individual banks operating in Pakistan. These levels of efficiency are also analyzed under CAMELS indicators to provide micro insights of their financial standings to justify their prevailing positions. The results show that banks are significantly distinct at different efficiency levels ranging from 87 percent to 49 percent. Technology has played a significant role in reducing the cost of banking industry. However, the banking industry is still operating under diseconomies of scale. Moreover, non-performing loans have adversely impacted the cost structure of banking industry. CAMELS ratios indicate that the most efficient banks are those with lesser amount of non-performing loans, high capital adequacy, lesser non-interest expenditure which leads to high profitability.*

*JEL Codes: D21, D61, G21*

*Key Words: Cost Efficiency, Diseconomies of Scale, Non-Performing Loans, CAMELS Ratios, Pakistan*

### **1. Introduction**

The objective of this paper is to undertake an empirical investigation of relative cost efficiency of individual banks operating in Pakistan. The study focuses on the banking industry due to its predominant role in Pakistan's financial sector, with a 67.8 percent share in the total assets of the financial system.<sup>1</sup> It is assumed that all banks are operating under similar kind of macroeconomic environment, prudential

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<sup>1</sup> See, State Bank of Pakistan (2002).

regulations, and external spillover.<sup>2</sup> Therefore, having made these assumptions, it will be interesting to investigate the factors, other than the aforementioned variables, which contribute to place them at distinct efficiency levels. Moreover, the opening of a number of banks and privatization of some weak performing public sector banks in the early 90s, as a result of financial sector reforms, boosted the competitive environment in the banking industry. This accelerated competition prompted banks to achieve high cost efficiency for their survival in the banking industry.

As cost competitiveness and financial health are important factors in determining the cost efficiency/inefficiency of banks, this study estimates the distinct efficiency level of each bank through an appropriate frontier approach and assesses its financial health through various financial indicators. It will also be worthwhile to explore if cost competitive banks are also financially healthy. Therefore, this study uses CAMELS<sup>3</sup> ratios, financial indicators to assess financial health, to justify the financial analysis of distinct efficient banks. These ratios will give a clear vision of financial soundness and indigenous strengths of banks by detailing various aspects of capital adequacy, asset quality, management capability, earning capacity, liquidity, and sensitivity to risk.

The last decade, especially the second half, is characterized by various advanced technological adoptions by banks; for example, E-Banking, Automated Teller Machines (ATMs), Credit Cards, Society for Worldwide International Facilitation Transfers (SWIFT), National Institutional Facilitation Technologies (NIFT), etc. The aim of adopting advanced technologies, despite bearing the heavy fixed cost for it, was to speed up the process of financial transactions through broad automated networking that resulted in low transaction cost per unit as well as customer facilitation in terms of fast human interaction. To empirically capture that, the present study also attempts to quantify the impact of technology on per unit average cost of the banking industry.

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<sup>2</sup> The statement is assumed to generally hold for the cost-affecting determinants of banking industry. For example, banks are dealing in same loan markets, stock exchange volatility, provisioning standards, minimum paid up capital requirement, Cash Reserve Requirement (CRR), Statutory Liquidity Ratio (SLR) etc. However, some exceptions can not be negated. For example, some public sector banks received liquidity injection after 2000 for being too big to fail which might had not been the case for others. Similarly, some foreign banks have pre-determined business strategies implied by their parent banks. For example, some foreign banks are restricted to invest in volatile stock market but at the same time have liquidity cushion from their parent bank.

<sup>3</sup> CAMELS: C = Capital, A = Assets, M = Management, E = Earnings, L = Liquidity, S = Sensitivity to Risk.

Until the recent past, the huge amount of non-performing loans (NPL) has been a serious concern to the banking management as well as to financial regulators. Whereas the NPL portfolio is still substantial, its growth has been minimized due to financial sector reforms. These infected loans swallow the profitability, as they become part of losses (and hence expenses) after passing through the standard provisioning cycle. Therefore, this study also attempts to quantify the impact of NPLs upon the cost structure of banks. Moreover, the expanded business portfolio, especially of large-sized banks, points towards a serious concern: are banks potentially compliant with expanded business activities? In literature, this concern has been widely analyzed through estimating economies of scale that has been included in this study.

A number of studies have analyzed various aspects of cost efficiencies including scale efficiency, scope efficiency, allocative efficiency, technical efficiency, pure technical efficiency etc. [Burki and Niazi (2003), Berger (1993), Berger and Mester (1997), Humphrey and Pulley (1997), Sathye (2001)].<sup>4</sup> With reference to Pakistan, in the light of immense degree of financial sector reforms and structural changes in the ownership of Pakistani banking industry, some studies conclude that large-sized banks (which are mostly public sector banks in Pakistan) are relatively more cost efficient than small-sized banks (mostly foreign and private commercial banks) [Imi (2004), Iimi (2002), Hardy and Patti (2001), Burki and Niazi (2003)].

Most of the previous studies estimate cost, profit, or revenue efficiencies of specific groups of banks rather than those of individual banks. In this way, one or group of some out-performing bank(s) may supersede the dismal efficiency levels of the remaining banks of the same group presenting a misleading picture of that particular group. However, this study estimates the efficiency level of all individual banks in the sample to avoid the problem of dominance of one bank over others within the same group. The efficiency estimates of all individual banks are further analyzed with various CAMELS ratios to strengthen the analysis.

The study is organized as follows. Section 2 discusses the theoretical framework of estimating efficiency levels. It also includes the various approaches used to define inputs/outputs specific to the intermediary nature of banks. Section 3 describes the methodology including a brief description of various parametric/non-parametric approaches of estimation. Section 4 details the technical interpretations of empirical results. Section 5 analyzes the extreme groups of efficient/inefficient

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<sup>4</sup> Some studies also measure the profit and revenue efficiency [Hardy and Patti (2001)].

banks with the help of CAMELS indicators, which differentiates this study from others. Conclusion follows in section 6.

## **2. Theoretical Underpinnings of Estimating Cost Efficiency of Banking Industry**

*A bank is cost efficient if it produces the given level of output(s) using the mix of given inputs at minimum possible cost.*

Estimating cost efficiency is based upon the observed cost values of any firm relative to the best practicing firm. Therefore, cost efficiency is defined as the ratio between the minimum cost  $C^*$ , at which a firm can produce a given vector of output, and actual cost  $C$ . Thus, cost efficiency  $CE = C^*/C$  implies that it would be possible to produce the same vector of outputs with a saving in costs of  $(1-CE)$  percent. The best practicing firm is, by assumption, operating at 100 percent efficiency level, as  $CE$  for best practice firms is 1. It is important to note that achieving 100 percent cost efficiency is a relative measure by comparing best practice firms with others. Therefore, the relative cost efficiency will exist within the range of 0 to 100 percent.

Theoretically, cost of any specific bank may deviate from that of the best-practice bank due to two main factors: uncontrollable random shocks and controllable bank specific cost inefficiencies. The uncontrollable random shocks include internal/external shocks, accounting errors, amendments in policy vector,<sup>5</sup> and a number of other factors. The controllable cost inefficiencies can be a function of administrative mismanagements, non-optimal diversification of assets portfolio, misallocation of inputs, and so forth.

Cost inefficiency has been further categorized into four inefficiencies: scale inefficiency, scope inefficiency, technical inefficiency, and allocative inefficiency. Scale inefficiency takes place as a consequence of producing non-optimal level of output(s). Scope inefficiency exists on account of producing non-optimal mix of outputs. Technical inefficiency is associated with wastage of inputs and allocative efficiency takes place due to selecting wrong combination of inputs.

Another important issue is to determine the vector of inputs/outputs of banks in the light of their financial intermediary nature. Theoretically, inputs/outputs of banks can be classified under two broad approaches: (a) production approach, and

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<sup>5</sup> For example, imposed restriction to increase capital base or change in tax policy, etc.

(b) intermediation approach. According to the “production approach,” banks use capital and labor as inputs to produce individual accounts of various sizes and incur operating cost in the process. Operating costs are incurred in the course of processing deposits and loan documentation. Therefore, the number of deposits and loan accounts is, according to this approach, a measure of bank’s output, while average account size is used as proxy to the characteristics of this output. Consequently, total bank cost in this approach includes only operating costs by excluding interest costs. However, according to “the intermediation approach,” banks collect deposits and purchased funds from outer sources, and use them as a source of generating earning assets such as loans, bonds and shares, etc. The latter approach considers earning assets as a proxy to bank’s outputs while deposits, capital, and labor as its inputs.

This study uses intermediation approach and evaluates the cost efficiency of individual banks operating in Pakistan. The production approach is preferable when the aim is to investigate operational cost efficiency of banks. As intermediation approach only incorporates average account size, it is not possible to analyze the implications of a large number of small accounts since outputs are computed as outstanding amounts.

### **3. Methodology**

It is of prior importance to estimate the cost frontier of best-practicing bank(s) to further assess the relative cost efficiencies of other banks. In this regard, various econometric approaches have been used including parametric approaches (stochastic frontier approach, thick frontier approach and distribution free approach) as well as a non-parametric approach (data envelopment approach).

Broadly speaking, these approaches differ in distributional assumptions of residual terms. The Stochastic Frontier Approach (SFA) assumes that inefficiency follows an asymmetric half-normal distribution, while random errors follow a symmetric normal distribution. The Thick Frontier Approach (TFA) follows the same distributional assumptions as SFA but estimates average cost of the efficient quartile of banks as cost frontier instead of a single best practicing bank in order to reduce the effect of probable exceptions (outliers banks). The impact of these exceptions may be more probabilistic and hence problematic in assessing the true relative efficiencies level in SFA. Moreover, TFA assumes inter quartile deviations as random errors while intra quartile as cost inefficiencies. Berger (1993) found that when the inefficiencies were unrestricted, the efficiencies were much more like symmetric normal distributions than half normal (as in SFA). By using the panel data, some of the maintained distributional assumptions in the

SFA can be relaxed and this approach can be termed as Distribution Free Approach (DFA). The Data Envelopment Approach (DEA) assumes that there are random fluctuations, so that all deviations from the estimated frontier represent inefficiency. If there is any measurement error in an observation not on the estimated frontier, it will be mistakenly included in that firm's measured efficiency. If there is a random error in an observation on the frontier, it will be mistakenly reflected in the measured efficiency of all firms that are measured relative to that part of the frontier. The choice of any specific approach depends upon the research objectives and available data. However, the non-parametric approach is highly sensitive to outliers as parametric models are considered relatively more robust.

This study uses DFA to estimate the relative cost inefficiencies of individual banks operating in Pakistan by using the panel data from 1991 to 2002. In DFA, estimated inefficiencies are assumed to be stable over the sample period while random errors average out. Moreover, this study uses Fixed Effect Model (FEM) as the panel data enables standard models of fixed and random effects to be estimated without any prior assumptions about the distribution of inefficiency terms, provided that efficiency is constant over time [Schmidt and Sickles (1984)].

Banks usually generate earning assets through financial intermediation. Therefore, the cost structure of banks can be classified as a function of vector of output (earning assets), vector of input prices, random error, and level of inefficiency as in the following equation:

$$C = f(Y, W) + u + v \quad (1)$$

Where  $C$  is abbreviated for total cost,  $Y$  represents vector of outputs,  $W$  indicates vector of inputs prices,  $v$  signifies random error and  $u$  level of inefficiency of banks. The residual terms of the model are decomposed into two terms: one indicates the level of inefficiency ( $u$ ) while the other represents random errors ( $v$ ).

In measuring cost inefficiencies, there is a problem with isolating inefficiency terms from random errors in the model. To overcome this problem, this study uses FEM in which the bank's specific constant incorporates the inefficiency elements associated with that specific bank.

Here, one can question the justification of the choice of random effect or fixed effect model as an appropriate choice. There are also some standard statistical tests

that help in choosing random or FEM based on consistency criteria.<sup>6</sup> However, the choice of random effect model is more appropriate when the sample is randomly drawn from the population. In this case, the individual effects are expected to have more exposure to random elements and subjected to volatility depending upon the change in the range and time interval of the sample size. On the contrary, if the inferences are based on population, the FEM is an appropriate choice where individual effects are invariant of time. The sample of this study covers almost the entire banking cluster; therefore, the choice of FEM will be an appropriate one.

The following econometric equation represents the generic form of the model:

$$C_{it} = \alpha + \beta X_{it} + u_i + v_{it} \quad (2)$$

Where  $i = 1, 2, \dots, N$  indexes the 37 included banks,  $t = 1, 2, \dots, T$  indexes the time period from 1991 to 2002,  $C_{it}$  symbolizes total cost of  $i^{th}$  bank at time  $t$ ,  $v_{it}$  represents random errors associated with  $i^{th}$  bank at time  $t$  and  $u_i$  indicates inefficiency level of  $i^{th}$  bank which is assumed to remain constant over time. Similarly,  $X_{it}$  represents the vector of exogenous variables. It is important to recall that the efficiency associated with each bank remains stable over time in FEM.<sup>7</sup>

The random errors and efficiency terms have the following assumptions:

- The  $v_{it}$  term is uncorrelated with the regressors  $X_{it}$  such as  $\text{corr}(X_{it}, v_{it}) = 0$
- The inefficiency level of best practice banks (as a bench mark) is assumed zero at any point of time.
- $u_i$ s are assumed to follow identically independent distribution (*iid*) with mean  $\mu$  and variance  $S_u^2$ .
- $\text{Corr}(u_i, v_i) = 0$

By using FEM, it is assumed that the differences in intercepts are driven by distinct level of inefficiencies associated with each bank. The impact of exogenous

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<sup>6</sup> For example, the Hausman Test.

<sup>7</sup> The stable inefficiencies over the whole sample period have been criticized on the ground that it reflects the adoption of consistent administrative and financial measures regardless of the prevalent efficiency level [Maudos and Pastor (2003)].

variables upon cost structure is taken as same for all banks. This can be justified by the fact that all banks are operating under the same macroeconomic conditions, prudential regulations, imposed fiscal restrictions, and external effects. Therefore, the general format of model given in Equation (2) can be modified as:

$$C_{it} = (\alpha + u_i) + \beta X_{it} + v_{it} \quad (2a)$$

Where,  $\alpha_i = \alpha + \mu_i$  . or,

$$C_{it} = \alpha_i + \beta X_{it} + v_{it} \quad (2b)$$

The associated difference in inefficiency for each bank has led  $a_i$  to be different for all banks.

Equation (2a) estimates separate intercepts of individual banks by assuming that best practice bank is 100 percent efficient having minimum intercept in magnitude such that  $\alpha_{\min} = \alpha_1 + \mu_1 = \alpha_1 + 0 = \alpha_1$  . Given that estimated model is expressed in log form, the relative inefficiencies of remaining individual banks,  $a_i$  , can be computed by using their respective estimated intercepts such as  $\mu_i^{\wedge} = \alpha_i - \alpha_{\min}$  . The estimate of intercepts and  $\mu_i$  are asymptotically consistent [Schmidt and Sickles (1984)].

The expression of efficiency can be computed by following the given expression:

$$E_i = (C_{\min} / C_i) = \exp(-\mu_i) = \exp(\alpha_i - \alpha_{\min}) \quad (2c)$$

The proxies of inputs/outputs of banks are consistent with the definition of intermediation approach as discussed earlier. This study is based upon unbalanced micro panel data of 37 banks operating in Pakistan from 1991 to 2002.<sup>8</sup> The data is obtained from the published audited balance sheets of individual banks on annual frequency. The balance sheets published other than annual frequencies are adjusted taking time as adjustment parameter. These 37 banks consisted of 92.64 percent capital, 92.25 percent assets, 91.48 percent expenses, 92.9 percent employment, 98.87 percent deposits and 87.58 percent advances of the banking

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<sup>8</sup> This study does not have equal number of observations for all banks and thus panel data set used in this study is unbalanced.



industry. Therefore, it would be fair to assume that data coverage of banking sample size represents almost the whole banking industry.

There are some Non-Bank Financial Institutions (NBFIs) operating in Pakistan that collect time and saving deposits and make loan disbursement in some particular targeted markets. These institutions include Development Financial Institutions (DFIs), Leasing Companies (LCs), Modaraba Companies (MCs), Housing Finance Companies (HFCs) etc. This study, however, does not include these institutions due to five reasons. First, these institutions are not permitted to collect current deposits, which make their cost of funding unparallel to banks. Second, at their individual status, these institutions have quite a small share in total financial sector, which, probably, would not allow efficiencies of these intuitions comparable with banks. Third, due to having a small pool of funds, these companies could not succeed in attracting big corporate and blue chip firms that have led their financing scope highly limited. Their loans disbursements are mostly subject to markets, which are residuals for banking industry and mainly include Small and Medium Enterprises (SMEs). These segregated market advocates not to compare the efficiencies of the two, the banks and NBFIs. Fourth, the Prudential Regulations (PRs) for these institutions set by Security and Exchange Commission of Pakistan (SECP) differ from banks. Fifth, the objective and motivation of businesses of NBFIs have been defined entirely different from those of banks.

The traditional U-shaped long-run average cost curve suggests following a second order polynomial functional form to approximate the true cost function. Most of the studies, which have conducted empirical investigations on banking cost, use transcendental logarithmic (trans log) cost function, which is a second order polynomial approximation of true cost function at any arbitrary point. Moreover, it is quite flexible as it captures the impact of cross independent variable terms (cross effects) on dependent variable.

The trans log cost function of an  $i^{\text{th}}$  bank following FEM is expressed in Equation (3) below:

$$\begin{aligned}
 TC_{it} = & \alpha_i + \sum_{j=1}^2 \beta_j Y_{jit} + \sum_{k,j=1,k \leq j}^2 \beta_{kj} Y_{kit} Y_{jit} + \sum_{l=1}^3 \gamma_l W_{lit} + \sum_{m,l=1,m \leq l}^3 \gamma_{ml} W_{mit} W_{lit} + \sum_{j=1,l=1}^{j=2,l=3} \delta_{jl} Y_{jit} W_{lit} \\
 & + \lambda (NPL / ASSETS)_{it} + \sum_{j=1}^2 \xi_j T Y_{jit} + \sum_{l=1}^3 \xi_l T W_{lit} + \xi T + e_{it}
 \end{aligned}
 \tag{3}$$

The given model estimates the unknown coefficients following the symmetry restriction:  $\beta_{ij} = \beta_{ji}$ ,  $\gamma_{ij} = \gamma_{ji}$ ,  $\delta_{ij} = \delta_{ji}$ .

In order to normalize the effect of differences in banks' sizes, all variables are expressed in ratios of total assets. The list of variables used in the model is as follows:

- $TC$  = Total cost (administrative cost plus interest expenses) to total asset ratio
- $Y_1$  = Ratio of total outstanding amount of loan and advances to total assets
- $Y_2$  = Ratio of total investment to total assets
- $NPL / ASSETS$  = percentage ratio of NPL to assets
- $W_1$  = Price of financial capital calculated as the ratio of total interest expenses to total deposits and financial borrowing
- $W_2$  = Price of physical asset calculated as the ratio of depreciation cost to total operating fixed assets
- $W_3$  = Price of labor input, calculated as the ratio of salary expenses to total number of employees.
- $i$  = Index of banks
- $t$  = Time subscript indicating the respective year, where  $t = 1, 2, \dots, 12$ .
- $T$  = Time variable quantifies the impact of technological progress upon cost.

Note that all the above variables are expressed in natural logs excluding NPL/Asset ratio and T.

#### 4. Estimation and Analysis of Empirical Results

The trans log cost function [Equation 3] is estimated using FEM assuming that residuals follow all fundamental assumptions of DFA as stated above (see, Table 1). Total expenses to total assets ratio is used as dependent variable while percentage of advances to assets, percentage of investment to assets, annual salary per employee (labor price), depreciation cost per million of operating fixed asset (price of physical capital) and interest expenses per million of borrowed funds (price of financial capital) are used as key independent variables. Moreover, the model is estimated by adding the percentage of NPLs to total asset ratio and time dummy as an independent variable.

**Table 1. Regression Estimates of the Model**

Variable	Coefficient	Std. Error	t-Statistic	Prob.
Dependent variable: Cost/Asset				
Method: Pooled Least Squares				
Sample (adjusted): 1991 2002				
Included observations: 12 after adjusting endpoints				
Number of cross-sections used: 36				
Total panel (unbalanced) observations: 338				
Convergence achieved after 7 iteration(s)				
Cross sections without valid observations dropped				
Advances	-0.56	0.31	-1.84	0.07
Advances^2	0.00	0.03	-0.05	0.96
Investment	-0.16	0.18	-0.90	0.37
Investment^2	0.00	0.01	0.35	0.72
Salary	0.95	0.37	2.56	0.01
Salary^2	0.02	0.04	0.60	0.55
Price (Financial capital)	1.86	0.44	4.18	0.00
Price (Financial capital)^2	0.00	0.05	-0.01	0.99
Price (Physical capital)	0.32	0.21	1.52	0.13
Price (Physical capital)^2	0.00	0.00	0.30	0.77
Advances*Investment	0.01	0.04	0.23	0.82
Salary*Price (Financial Capital)	0.14	0.06	2.25	0.03
Salary*Price (Physical Capital)	0.03	0.03	1.04	0.30
Price(Financial Capital)*Price Physical Capital	-0.02	0.04	-0.49	0.62
Advances*Salary	-0.04	0.07	-0.54	0.59
Advances*Price (Financial Capital)	-0.21	0.09	-2.35	0.02
Advances*Price (Physical Capital)	-0.08	0.04	-1.96	0.05
Investment*Salary	-0.06	0.02	-2.31	0.02
Investment*(Price Financial Capital)	0.00	0.03	-0.14	0.89
Investment*(Price Physical Capital)	0.02	0.02	0.89	0.37
Time Dummy (T)	-0.17	0.06	-2.76	0.01
Non Performing Loans (NPLs)	0.00	0.00	3.94	0.00
T*Advances	0.01	0.01	0.60	0.55
T*Investment	0.01	0.01	1.88	0.06
T*Salaries	-0.01	0.01	-1.40	0.16
T*Price (Physical Capital)	-0.01	0.01	-1.84	0.07
T*Price( Financial Capital)	-0.03	0.01	-2.26	0.02
$\alpha_{1-DPB}$	7.83	1.22	6.40	0.00
$\alpha_{2-DPB}$	7.86	1.22	6.46	0.00
$\alpha_{3-DPB}$	7.86	1.22	6.43	0.00
$\alpha_{4-DPB}$	8.07	1.22	6.60	0.00

Cont...

Table 1 Concluded

Variable	Coefficient	Std. Error	t-Statistic	Prob.
$\alpha$ 5-DPB	7.80	1.22	6.37	0.00
$\alpha$ 6-DPB	7.79	1.22	6.36	0.00
$\alpha$ 7-DPB	7.78	1.23	6.34	0.00
$\alpha$ 8-DPB	7.78	1.22	6.35	0.00
$\alpha$ 9-DPB	8.03	1.24	6.50	0.00
$\alpha$ 10-DPB	7.84	1.23	6.40	0.00
$\alpha$ 11-DPB	7.96	1.23	6.49	0.00
$\alpha$ 12-DPB	8.07	1.22	6.60	0.00
$\alpha$ 13-DPB	8.13	1.22	6.66	0.00
$\alpha$ 14-FPB	7.75	1.23	6.31	0.00
$\alpha$ 15-FPB	7.87	1.23	6.40	0.00
$\alpha$ 16-FPB	7.92	1.23	6.46	0.00
$\alpha$ 17-FPB	7.79	1.23	6.32	0.00
$\alpha$ 18-FPB	7.84	1.22	6.41	0.00
$\alpha$ 19-FPB	7.91	1.22	6.49	0.00
$\alpha$ 20-FPB	7.81	1.23	6.37	0.00
$\alpha$ 21-FPB	7.89	1.23	6.43	0.00
$\alpha$ 22-FPB	7.54	1.20	6.28	0.00
$\alpha$ 23-FPB	7.80	1.23	6.36	0.00
$\alpha$ 24-FPB	7.80	1.22	6.37	0.00
$\alpha$ 25-FPB	7.91	1.22	6.46	0.00
$\alpha$ 26-FPB	7.81	1.23	6.38	0.00
$\alpha$ 27-FPB	7.83	1.23	6.39	0.00
$\alpha$ 28-FPB	7.81	1.23	6.36	0.00
$\alpha$ 29-FPB	7.82	1.23	6.33	0.00
$\alpha$ 30-FPB	7.68	1.22	6.30	0.00
$\alpha$ 31-FPB	7.81	1.22	6.42	0.00
$\alpha$ 32-PSB	8.01	1.23	6.52	0.00
$\alpha$ 33-PSB	8.26	1.24	6.66	0.00
$\alpha$ 34-PSB	7.87	1.22	6.43	0.00
$\alpha$ 35-PSB	8.05	1.23	6.53	0.00
$\alpha$ 36-PSB	7.99	1.22	6.54	0.00
$\alpha$ 37-PSB	8.05	1.22	6.62	0.00
R-squared	0.84	Mean dependent var		2.23
Adjusted R-squared	0.80	S.D. dependent var		0.28
S.E. of regression	0.12	Sum squared resid		4.27
F-statistic	22.96	Durbin-Watson stat		2.01
Prob (F-statistic)	0.00			

DPB=Domestic Private Bank  
 FPB=Foreign Private Bank  
 PSB=Public Sector Bank

Equation (3) is a specific version of Equation (2) transformed into trans log cost function to estimate the relative cost efficiency of all individual banks in the sample. The relative inefficiencies' measures mainly rely upon estimated values of intercepts for each bank. All intercepts are statistically significant at 99 percent level of confidence. The adjusted  $R^2$  is 0.80 showing that 80 percent variations in the cost structure of banking industry are explained by given exogenous variables. F-statistic value is 22.96, which signifies the model in explaining cost structure of banking industry. It is generally argued that the DW test for panel data may come out with misleading results as it is biased towards 2. This biasness could be even more severe in the presence of panel data of relatively shorter time period. Therefore, the residuals of all individual banks are separately tested for AR (1). The results do not find serial correlation in any individual bank except for Bank 10 (Table 2).

The list of relative cost efficiency of all banks (Table 3) depicts that Bank 22, a foreign private bank (FPB), is the best practice bank and estimated as a cost frontier while the relative efficiencies of other banks fall within the range of 87 percent (Bank 30-FPB) to 49 percent [Bank 33- Public Sector Bank (PSB)].<sup>9</sup> The 49 percent relative efficiency of Bank 33 means that this bank could have saved 51 percent cost in producing the current level of earning assets by eliminating the element of cost inefficiency. The average relative efficiency of top 5 best practice banks is 85.3 percent corresponding to 56.6 percent for 5 least efficient banks. The overall average efficiency level of banking industry is found to be 72 percent which depicts that there is great room in banking industry to minimize cost by eliminating the elements of inefficiencies. In order to justify the time invariant condition of relative efficiencies which is an in-built property of fixed effects of the model, the model is estimated various times for different time spans. These repeatedly estimated results advocate that the relative efficiency levels of banks, more or less, maintain their respective places. This indicates not only the high robustness of the model but also its consistency with time invariant assumption of fixed effects.

The differences in efficiencies associated with each bank may be characterized by differences in administrative practices, choice in asset portfolios, risk management, labor skills, wastage of resources, share of infected loans, over staffing, and various other factors.

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<sup>9</sup> Efficiency level for Bank V (a Foreign Private Bank) is assumed 100 percent.

**Table 2. Regression Estimates of Residuals of Individual Banks for AR (1)**

	<b>Variable</b>	<b>Coefficient</b>	<b>Std. Error</b>	<b>t-Statistic</b>	<b>Prob.</b>
Bank 1	AR (1)	0.71	0.47	1.50	0.18
Bank 2	AR (1)	0.19	0.41	0.47	0.65
Bank 3	AR (1)	0.33	0.41	0.81	0.44
Bank 4	AR (1)	-0.42	0.30	-1.39	0.21
Bank 5	AR (1)	-0.17	0.77	-0.22	0.84
Bank 6	AR (1)	0.18	0.55	0.32	0.76
Bank 7	AR (1)	0.05	1.04	0.05	0.97
Bank 8	AR (1)	0.13	0.38	0.34	0.74
Bank 9	AR (1)	0.15	0.55	0.27	0.81
Bank 10	AR (1)	-0.57	0.27	-2.12	0.09
Bank 11	AR (1)	-0.18	0.43	-0.42	0.69
Bank 12	AR (1)	0.41	0.32	1.27	0.24
Bank 13	AR (1)	0.09	0.37	0.25	0.81
Bank 14	AR (1)	-0.35	0.34	-1.02	0.34
Bank 15	AR (1)	0.29	0.38	0.76	0.47
Bank 16	AR (1)	0.38	0.45	0.85	0.42
Bank 17	AR (1)	0.12	0.32	0.36	0.73
Bank 18	AR (1)	-0.55	0.44	-1.23	0.29
Bank 19	AR (1)	0.22	0.34	0.63	0.55
Bank 20	AR (1)	0.01	0.33	0.02	0.99
Bank 21	AR (1)	-0.12	0.35	-0.35	0.74
Bank 23	AR (1)	0.40	0.32	1.24	0.25
Bank 24	AR (1)	0.37	0.76	0.49	0.64
Bank 25	AR (1)	0.24	0.40	0.60	0.57
Bank 26	AR (1)	-0.05	0.40	-0.12	0.91
Bank 27	AR (1)	0.27	0.39	0.69	0.52
Bank 28	AR (1)	0.32	0.37	0.86	0.42
Bank 29	AR (1)	0.16	0.47	0.35	0.74
Bank 30	AR (1)	-0.20	0.45	-0.44	0.68
Bank 31	AR (1)	-0.16	0.37	-0.43	0.69
Bank 32	AR (1)	-0.17	0.32	-0.54	0.61
Bank 33	AR (1)	0.15	0.38	0.40	0.70
Bank 34	AR (1)	-0.02	0.37	-0.05	0.96
Bank 35	AR (1)	0.01	0.35	0.03	0.98
Bank 36	AR (1)	-0.23	0.33	-0.71	0.50
Bank 37	AR (1)	-0.37	0.33	-1.12	0.30

**Table 3. List of Relative Efficiency Estimates**

<b>Banks</b>	<b>Intercept</b>	<b>Intercept Value</b>	<b>S.E</b>	<b>t. Stats</b>	<b>Efficiency</b>
Bank 22-FPB	C <sub>V-FPB</sub>	7.54	1.20	6.28	100.00
Bank 30-FPB	C <sub>AD-FPB</sub>	7.68	1.22	6.30	87.03
Bank 14-FPB	C <sub>N-FPB</sub>	7.75	1.23	6.31	81.63
Bank 8-DPB	C <sub>H-DPB</sub>	7.78	1.22	6.35	79.11
Bank 7-DPB	C <sub>G-DPB</sub>	7.78	1.23	6.34	78.62
Bank 6-DPB	C <sub>F-DPB</sub>	7.79	1.22	6.36	78.43
Bank 17-FPB	C <sub>Q-FPB</sub>	7.79	1.23	6.32	78.29
Bank 24-FPB	C <sub>X-FPB</sub>	7.80	1.22	6.37	77.76
Bank 23-FPB	C <sub>W-FPB</sub>	7.80	1.23	6.36	77.21
Bank 5-DPB	C <sub>E-DPB</sub>	7.80	1.22	6.37	77.07
Bank 31-FPB	C <sub>AE-FPB</sub>	7.81	1.22	6.42	76.86
Bank 20-FPB	C <sub>T-FPB</sub>	7.81	1.23	6.37	76.67
Bank 28-FPB	C <sub>AB-FPB</sub>	7.81	1.23	6.36	76.45
Bank 26-FPB	C <sub>Z-FPB</sub>	7.81	1.23	6.38	76.41
Bank 29-FPB	C <sub>AC-FPB</sub>	7.82	1.23	6.33	76.13
Bank 27-FPB	C <sub>AA-FPB</sub>	7.83	1.23	6.39	75.00
Bank 1-DPB	C <sub>A-DPB</sub>	7.83	1.22	6.40	74.78
Bank 18-FPB	C <sub>R-FPB</sub>	7.84	1.22	6.41	74.31
Bank 10-DPB	C <sub>J-DPB</sub>	7.84	1.23	6.40	74.20
Bank 3-DPB	C <sub>C-DPB</sub>	7.86	1.22	6.43	72.97
Bank 2-DPB	C <sub>B-DPB</sub>	7.86	1.22	6.46	72.86
Bank 15-FPB	C <sub>O-FPB</sub>	7.87	1.23	6.40	72.36
Bank 34-PSB	C <sub>AH-PSB</sub>	7.87	1.22	6.43	71.93
Bank 21-FPB	C <sub>U-FPB</sub>	7.89	1.23	6.43	70.75
Bank 25-FPB	C <sub>Y-FPB</sub>	7.91	1.22	6.46	69.44
Bank 19-FPB	C <sub>S-FPB</sub>	7.91	1.22	6.49	69.31
Bank 16-FPB	C <sub>P-FPB</sub>	7.92	1.23	6.46	68.38
Bank 11-DPB	C <sub>K-DPB</sub>	7.96	1.23	6.49	66.08
Bank 36-PSB	C <sub>AJ-PSB</sub>	7.99	1.22	6.54	64.15
Bank 32-PSB	C <sub>AF-PSB</sub>	8.01	1.23	6.52	62.78
Bank 9-DPB	C <sub>I-DP</sub>	8.03	1.24	6.50	61.69
Bank 35-PSB	C <sub>AI-PSB</sub>	8.05	1.23	6.53	60.58
Bank 37-PSB	C <sub>AK-PSB</sub>	8.05	1.22	6.62	60.55
Bank 4-DPB	C <sub>D-DPB</sub>	8.07	1.22	6.60	58.90
Bank 12-DPB	C <sub>L-DPB</sub>	8.07	1.22	6.60	58.84
Bank 13-DPB	C <sub>M-DPB</sub>	8.13	1.22	6.66	55.67
Bank 33-PSB	C <sub>AG-PSB</sub>	8.26	1.24	6.66	49.03

The relationship between cost and Non-Performing Loans (NPLs) may fall under the problem of endogeneity. For example, the high ratio of NPLs in total loan portfolio may lead bank to incur provision cost in order to maintain some standard

accounting norms. From the other side, the high cost of loan monitoring/screening after disbursements may reduce the ratio of NPLs in total advances portfolio. However, in later case, it is highly difficult to extract the exact amount of cost from the total cost dedicated to loan monitoring/screening especially when investigated for every individual bank. Moreover, the ratio of screening/monitoring cost in total cost is probable to have very small portion as more than 60 percent of total cost comprises interest expenses. In contrast, the impact of NPLs on total cost is not only quantifiable, knowing the standard provisioning ratios, but significant as well, as most of public sector banks had been accumulating huge portion of NPLs.

The results show that one percent increase in NPLs to assets ratio leads 0.05 percent increase in cost to asset ratio (Table 4). This result warns that the continuous acceleration in NPLs can hit the financial soundness and profitability of a bank leading it towards dismal financial health. The amount of NPLs is substantially lesser in the most efficient group of banks relative to the least efficient group [Fig 1(C)]. The least level of NPLs in total loan portfolio, as well as following the declining trend in efficient group, can be attributed to sound credit policies such as collateral standards, appropriate project feasibility, avoiding risky portfolios, and appropriate measures of hedging (for example, asset liability mismatch, exchange rate hedging, etc.).

The results indicate that the technological progress has helped banks in reducing cost enormously. During the sample period, technological progress was widely seen in automation and its subsequent up-gradation; for example, introduction of ATMs, Tele Banking, Internet Banking, Credit and Debit Cards, etc. These advanced modes of banking have helped banks to facilitate financial transaction at cheaper cost.

**Table 4. Cost Elasticity of Exogenous Variables**

Cost elasticity of advances	$\eta_C^{Advances}$	0.713
Cost elasticity of investment	$\eta_C^{Investments}$	0.091
Cost elasticity of physical asset price	$\eta_C^{price-physical}$	0.28
Cost elasticity of salary	$\eta_C^{Salary}$	0.57
Cost elasticity of interest rates	$\eta_C^{Price-Financial}$	0.70
Cost elasticity of NPLs	$\eta_C^{NPLs}$	0.05
Cost elasticity of Technology change	$\eta_C^{Time}$	-0.538



The economies of scale depict the percentage increase in the value of cost if all outputs increase by one percent in their value. It can be calculated as follows:

$$SE = \frac{1}{\sum_i \eta_{Y_i}} \dots\dots\dots \forall i = 1 \dots n \tag{4}$$

Where  $\sum_i \eta_{Y_i}$  represents the sum of cost elasticity of all individual outputs (advances and investment in this study). For being estimated from Trans log cost function which is second order Taylor approximation of true cost function, the estimates of scale economies is also an approximated value of true cost function. The  $SE > 1$  shows diseconomies of scale while  $SE < 1$  depicts economies of scale. SE is estimated to be 1.24 showing that the percentage increase in the value of cost is more than the percentage increase in the value of outputs. It can strongly be argued that resources of banking industry have been capitalized more than their potential. As expected, the large-size public sector banks are the most responsible participants for causing diseconomies of scale in the banking industry due to their huge balance sheet sizes. This study estimates scale inefficiency as one of the major causes driving inefficiency in the whole banking industry.

Despite the significant positive impact of salary upon cost, the most efficient banks offer high salaries to their employees as compared to the least ones. These attractive salary packages offered by efficient banks are associated with considerably high earning capacity of labor [Fig 1(E)]. In this scenario, it can be argued that most efficient banks are hiring comparatively skilled labor at high salaries and are capable in optimal resources allocation, market information utilization, and risk management.

**5. Cost Efficient/Inefficient Banks and CAMELS Indicators**

CAMELS ratios are mostly used to quantify the financial soundness and health of banks through micro analysis of balance sheets and income statement items. These ratios are commonly used by central banks and rating agencies which help them to envisage the earlier signals of prospective problems in the financial health of banks. These prospects, including various financial indicators, incorporate quality of assets, financial soundness, management quality, earning capacity of assets, liquidity position and risk taking behavior of banks. Therefore, it will be interesting to analyze the cost efficiency/inefficiency of these banks in relation to the CAMELS indicators. This study also analyzes two extreme groups derived from the regression analysis above, 5 best-cost efficient banks and 5 least cost-

efficient banks under the umbrella of CAMELS indicators to make the comparison more objective (Table 5).

**Capital Adequacy:** Capital adequacy provides insurance about financial soundness against unforeseen contingencies. It acts as a shield against expected losses associated with risk attached to banks. During the whole sample period, the cost-efficient group of banks remained under the compliance of high capital to liabilities ratio in comparison to low for least cost-efficient group [Fig 1(B)]. The high capital/liability ratio of efficient group is due to lesser amount of provisioning against bad debts as this group has lower ratio of bad debts in total loan portfolio. The provisioning against bad debts ultimately becomes part of losses and gets eroded from the capital base of the bank. In addition, consistent high profit is the source of continuous rise in the capital base of most efficient

**Table 5. Weighted Average of CAMELS Indicators of Efficient/Inefficient Groups of Banks**

	<u>Efficient Group</u>	<u>Inefficient Group</u>
<b>Capital Adequacy</b>		
Capital to risk weighted assets ratio	17.75	7.45
Capital to liability ratio	10.38	2.76
<b>Asset Quality</b>		
Non-performing loans to total loans	6.77	20.95
Earning assets to total assets ratio	72.74	77.38
<b>Management</b>		
Total expenditure to total income ratio	68.02	104.74
Operating expenditure to total expenditures	23.35	42.94
Earning per employee indicator*	7.70	0.92
Interest rate spread	3.72	4.43
Operating expense per employee*	1.23	0.40
<b>Earnings and Profitability</b>		
Net profit to asset ratio	0.67	-0.73
Net profit to equity ratio	11.22	-5.70
Net interest margin	2.63	3.43
Interest expense to total assets	6.46	5.10
Non-interest expense to total assets	1.87	4.30
Interest expense to total expenses	74.89	53.68
<b>Liquidity</b>		
Liquid assets to total assets ratio	40.91	38.68
<b>Other Indicators</b>		
Advances to total assets ratio	43.86	45.60
Investment to total assets ratio	24.05	29.03
Loan to deposit ratio	61.12	53.56

\* Rs.millions per employee

banks. The sharp decline of capital/liability ratio faced by the inefficient group in the mid-90s was observed due to imposed international provisioning standards. In addition, the cost efficient group also maintained a high percentage of capital to risk weighted assets corresponding to consistently poor ratio of the least efficient group [Fig 1(A)].<sup>10</sup> In fact, accelerating risky portfolio with weak credit policy in cost inefficient group resulted in a high percentage of risk weighted assets and erosion of capital base associated with bad debts.

**Asset Quality:** One of the most commonly used indicators for asset quality is NPLs to Total Loans (TL) ratio. Theoretically speaking, NPLs are directly related to cost of banks as NPLs become (after provisioning) part of the non-interest expense of banks. In addition, the empirical results of this study provide significant positive impact of NPLs on the cost of banks. This will be further elaborated if the NPLs/TL of two cost extreme groups is compared. The weighted average of NPL/TL of the efficient group is 6.76 against 20.95 percent of the least efficient group. The NPL/TL of the efficient group remained low and stable during the sample period against an accelerating trend in the inefficient group [Fig (1C)]. The lower percentage of NPLs/TL in the cost efficient group is in line with credit disbursement adopting sound collateral standards, strong credit policy, having a broader vision of evaluating risks, while taking least political interference and appropriate measures of hedging (for example, asset liability mismatch, exchange rate hedging, etc.).

The efficient cost group also concentrated at maintaining appropriate physical equipments and adopting advanced technology to run the business in a more feasible way which kept their non-earning asset to total assets ratio higher than the least efficient group. However, these non-earning assets are the potential assets, which are essential to enhance the earning capability of banks. For example, the non-earning assets mainly include the high value technological equipments (for example, ATM machines, soft wares, and computers), well-furnished and renovated offices, and other operating fixed assets.

**Management:** Management has an extremely vital role for banks to achieve their cost efficiency. The management decides the financing modes of banking operations, choice of asset portfolio, amount of risk taken and all operational strategies. It will be worthwhile to compare the management quality between most efficient and least efficient group of banks.

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<sup>10</sup> The calculation of Risk Weighted Assets started in 1997 under the prescribed rules of Basel II Accord.

The interest rate spread is an important and commonly used indicator for evaluating efficiency of banks. The lower intermediation cost will lead a bank to gain lesser interest rate spread. In this study, the weighted average of interest rate spread of efficient group is 3.72 percent against 4.42 percent in the inefficient group. It depicts that the reduced cost structure of cost efficient group has made them well capable in charging lesser amount of interest rate spread.

Another indicator for management, Operating Expenditures (OE) to Total Expenditures (TE) ratio, shows that OE/TE is much lower for the efficient group than the inefficient group. This implies that the cost efficient group has controlled and optimized operating expenditure in a more comprehensive way. The high portion of OE in TE of the least efficient group is associated with over sizing of employees leading to high salary expenses as well as using high portion of obsolete operating fixed assets thus incurring high depreciation cost. The earning per employee (EPE) of efficient group is higher and on rise against the extremely low and stable trend of inefficient group [Fig 1(E)].

It is probably because of the efficient group's choice of better human resource from the market, at highly attractive salary packages, which are competent in optimal resource allocation, market information utilization, and forecasting and risk evaluation. Furthermore, the operating expense per employee is higher and increasing in the efficient group and advocates that per employee coverage of banking operations is higher in the efficient group than in the inefficient group.

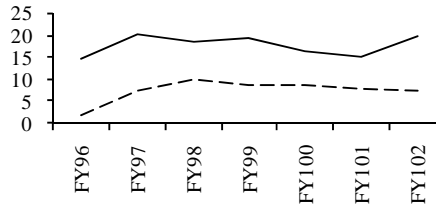
**Earnings and Profitability:** In the competitive banking environment, banks concentrate more on reducing cost than raising revenues to serve the rational of profit maximization. However, consistent income streams are also necessary which build the capital base of the bank. In this study, the cost efficient banks also have strong earnings and profitability.

The cost efficient banks contain a weighted average of profit to assets ratio as 0.67 against -0.73 of cost inefficient banks. Similarly, the net profit to equity ratio of cost efficient banks is 11.22 against -5.70 associated with the cost inefficient group.

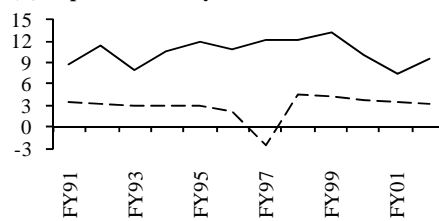
Cost efficient banks have attained a very low level of non-interest expense to total expense ratio, that is, 1.87 percent against 4.3 percent associated with the inefficient group. The lower ratio of cost efficient banks is in line with optimized

**Figure 1. Trends of Various CAMELS Ratios (in Percent)**

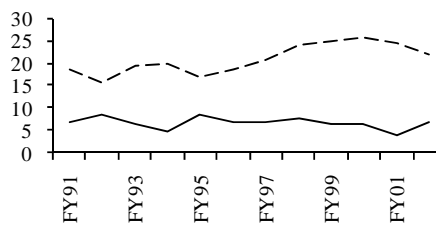
**(A) Capital to Risk Weighted Assets**



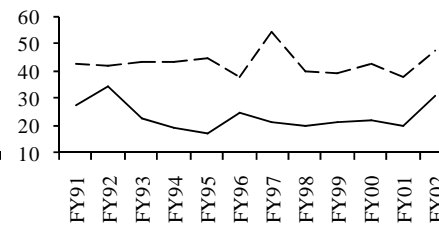
**(B) Capital to Liability Ratio**



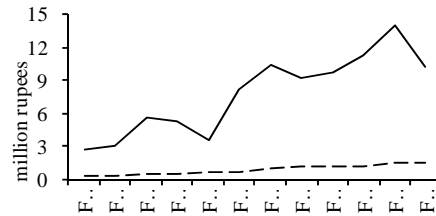
**(C) Non-Performing Loans to Total Loans**



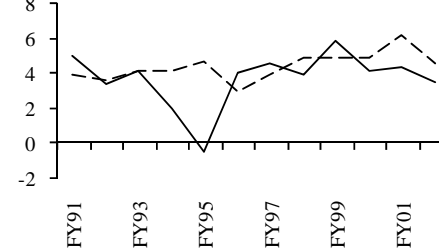
**(D) Operating Expenditures to Total Expenditures**



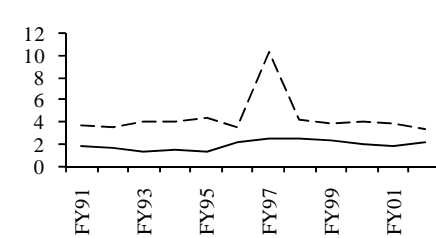
**(E) Earning per Employee**



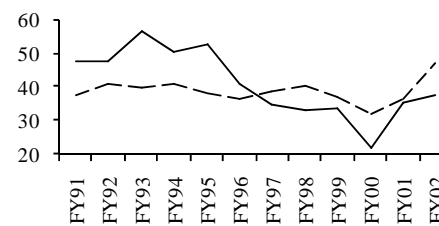
**(F) Interest Rate Spread**



**(G) Non-Interest Expense to Total**



**(H) Liquid Assets to Total Assets**



administrative cost and lesser amount of losses against NPLs. Interestingly, the interest expenses to total asset ratio is higher in the cost efficient group, which is 6.46 against 5.10 of the cost inefficient banks. This reflects that the efficient group is attracting depositors at higher interest rates.

**Liquidity:** Maintaining sufficient liquidity is necessary to meet the current and near future obligations. The efficient group is maintaining a higher portion of liquid asset in total assets (40.91 percent) than the inefficient group (38.68 percent). However, this ratio remained in a declining trend during the sample period for efficient banks, which is due to high expenditures made by this group in intangible fixed assets and technology.

## 6. Conclusion

This study has used the DFA by applying it on trans log model for the unbalanced panel data of 37 scheduled banks operating in Pakistan from 1991 to 2002. It is found that all banks significantly differ in relative cost efficiency ranging from 87 percent to 49 percent. Most of the public sector banks exist in the least efficient group while the majority of foreign banks and some private commercial banks in the best efficient group. NPLs have significantly enhanced the degree of cost inefficiency in the banking industry. In addition, these infected loans are also a considerable source of erosion of the capital base of banks, through standard provisioning against them, which has worsened the financial soundness of banks. The technological progress, which mainly comprised computerization and automation of financial transactions, has significantly reduced the cost of banking industry during the sample period. The banking industry is over-utilizing its resources and operating under diseconomies of scale as the marginal cost is 24 percent more than the real value addition.

The CAMELS indicators provide additional information about the sound and strong financial position of cost efficient banks. These strengths can be indicated by various financial ratios including high capital to liability ratio or capital to risk weighted assets ratio, lesser amount of non-performing loans to total loan ratio, lower expenditure to income ratio, lower operating expenditure to total expenditure ratio, etc. These financial ratios advocate that besides achieving cost efficiency, the cost efficient group has also maintained robust financial health which resulted in higher profitability and strong financial soundness. Moreover, the efficient group is associated with lesser interest rate spread, which is another sound indicator of efficiency.

Overall, there is scope for cost saving in the banking industry of Pakistan that can be achieved through adopting corrective measures in administrative management, optimal diversification of asset portfolio, technological progress, and reducing the amount of NPLs.

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